CSE 2021
COMPUTER ORGANIZATION

HUGH CHESSER
CSE B 1012U

W4-M

System Calls

Example # 1: Print a string

```
.data
     str:     .asciiz "the answer is"
.text
     addi $v0,$zero,4
     la $a0,str    # pseudoinstruction
     syscall
```

Example # 2: Input an integer

```
     addi $v0,$zero,5
     syscall
```

Example # 3: Print an integer

```
     addi $v0,$zero,1
     addi $a0,$s0,$zero
     syscall
```

Example # 4: Read String

```
     addi $v0,$zero,8
     la $a0,Buff  #$a0=address of Buff
     addi $a1,$zero,60 #$a1=max. len.
     syscall
```

Service	System Call Code ($v0)	Arguments	Result
print_int	1	$a0 = int	
print_float	2	$f12 = float	
print_double	3	$f12 = double	
print_string	4	$a0 = string address	
read_int	5		int (in $v0)
read_float	6		float (in $f0)
read_double	7		double (in $f0)
read_string	8	$a0 = buffer $a1 = length	
sbrk	9	$a0 = amount	address (in $v0)
exit	10		terminate prog

Putting it all together (2)

Activity: Write a MIPS program which does the following:

1. Accepts an integer N using the following prompt

   Please input a value for N =
2. Computes the sum of integers from 1 to N, i.e., (1 + 2 + … + N) if N > 0
3. Displays the result (X) as

   The sum of the integers from 1 to N is X
2. Waits for the next number N.
3. If N <= 0, the program exits with the following farewell

   Chao - Have a good day

Run the program in the spim simulator to verify the results

main routine

```
1  .data
2      str1:       .asciiz "\nPlease input a value for N = "
3      str2:       .asciiz "The sum of the integers from 1 to N is...\n\t\t\t"
4      str3:       .asciiz "\n\"Chao\" - Have a good day"
5  .text
6  main:
7      addi $v0,$zero,4
8      la $a0,str1          # pseudoinstruction
9      syscall              # Print out user prompt
10 #-----------------------------------------------
11     addi $v0,$zero,5     # input integer
12     syscall
13 #-----------------------------------------------
14     add $a0,$zero,$v0    # Move input integer as to $a0 - input to sum
15     slt $t0,$v0,$zero
16     bne $t0,$zero,end    # if input <0 end
17     jal sum              # Jump to subroutine sum
18 #-----------------------------------------------
19     addi $sp, $sp, -4
20     sw $v0, 4($sp)       # Put the sum on the stack
21     addi $v0,$zero,4
22     la $a0,str2
23     syscall              # Print message for sum
24 #-----------------------------------------------
25     addi $v0, $zero,1
26     lw $a0, 4($sp)       # Get sum from stack
27     addi $sp, $sp,4
28     syscall              # Print sum
29 #-----------------------------------------------
30 end:
31     addi $v0,$zero,4
32     la $a0,str3
33     syscall              # Print out good bye message
34     add $a0,$a0,$zero
35     addi $v0,$zero,17
36     syscall              # exit2
37 #-----------------------------------------------
```

sum subroutine

```
38 sum:
39     addi $sp, $sp, -8    # Set up the stack
40     sw $ra, 4($sp)       # Save return address
41     addi $t0, $a0, 0     # Initialize the sum
42     li $v0, 0            # Initialize return value
43     beq $t0,$zero, ret   # If argument is 0 then return
44     addi $t1, $t0, -1    # Compute n-1
45     sw $t0, 8($sp)       # Save caller saved regs
46     addi $a0, $t1, 0     # Move n-1 into argument register
47     jal sum              # Call sum
48 #-----------------------------------------------
49     lw $t0, 8($sp)       # Restore caller saved reg
50     add $v0, $t0, $v0    # Add return value to $t0
51     lw $ra, 4($sp)       # Get the return address
52     addi $sp,$sp,8
53 ret:
54     jr $ra               # Return
```

Agenda for Today

1. Addition, Subtraction
2. Overflow
3. Multiplication
4. Division
5. Floating Point: IEEE 754 single and double precision formats

Patterson: Sections 3.1 – 3.5

Addition and Subtraction

In MIPS, addition and subtraction for signed numbers use 2's complement arithmetic

Example 1: Add 10_{ten} and 15_{ten}

bit 1	bit 2	Prev. Carry	Sum	Next Carry
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

Table 1: Truth Table for addition

Example 2: Subtract 15_{ten} from 10_{ten}

Addition and Subtraction

In MIPS, addition and subtraction for signed numbers use 2's complement arithmetic

Example 1: Add 10_{ten} and 15_{ten}

Step 1: Represent the operands in 2's complement

10_{ten} = 0000 0000 0000 0000 0000 0000 0000 1010_{two}

15_{ten} = 0000 0000 0000 0000 0000 0000 0000 1111_{two}

Step 2: Perform bit by bit addition using table 1.

25_{ten} = 0000 0000 0000 0000 0000 0000 0001 1001_{two}

Example 2: Subtract 15_{ten} from 10_{ten}

The problem is reduced to $(10_{ten} + (-15_{ten}))$

10_{ten} = 0000 0000 0000 0000 0000 0000 0000 1010_{two}

-15_{ten} = 1111 1111 1111 1111 1111 1111 1111 0001_{two}

-5_{ten} = 1111 1111 1111 1111 1111 1111 1111 1011_{two}

bit 1	bit 2	Prev. Carry	Sum	Next Carry
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

Table 1: Truth Table for addition

Overflow (1)

Recall that:

Smallest signed integer: $1000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000_{two}$

$= -(2^{31})_{ten} = -2{,}147{,}483{,}648_{ten}$

Largest signed integer: $0111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111_{two}$

$= (2^{31} - 1)_{ten} = 2{,}147{,}483{,}647_{ten}$

What happens if the result of an operation is more than the largest signed integer or less than the smallest signed integer?

Example: Add $2{,}147{,}483{,}640_{ten}$ and 28_{ten}

28_{ten} $= 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0001\ 1100_{two}$

$2{,}147{,}483{,}640_{ten}$ $= 0111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1000_{two}$

$28_{ten} + 2{,}147{,}483{,}640_{ten}$ $= 1000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0001\ 0100_{two}$

$= -2{,}147{,}483{,}628_{ten}$

Overflow caused the value to be perceived as a negative integer

Overflow (2)

When can overflow occur?

Operation	Operand A	Operand B	Result indicating overflow
A + B	**A >= 0**	**B >= 0**	**< 0**
A + B	**A < 0**	**B < 0**	**>= 0**
A – B	**A >= 0**	**B < 0**	**< 0**
A – B	**A < 0**	**B >= 0**	**>= 0**

Integer Multiplication, Division

Both operations really imply a series of additions and subtractions

Example: Multiply 10_{ten} and 3_{ten}:

10_{ten} $= 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 1010_{two}$

3_{ten} $= 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0011_{two}$

$10_{ten} * 1_{ten}$ $= 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 1010_{two}$

$10_{ten} * 2_{ten}$ $= \underline{0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0001\ 0100}_{two}$

$= 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0001\ 1110_{two} = 0x1e = 30_{ten}$

Example: Divide 28_{ten} by 9_{ten}:

28_{ten} $= 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0001\ 1100_{two}$

9_{ten} $= 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 1001_{two}$

$$
\begin{array}{r}
11 \\
1001\overline{)11100} \\
\underline{1001} \\
1010 \\
\underline{1001} \\
1
\end{array}
$$

Floating Point: Single Precision

1. In MIPS, decimal numbers are represented with the IEEE 754 binary representation that uses the **normalized** standard scientific binary notation defined as

$$(-1)^{S} \times (1 + \text{fraction})_{\text{two}} \times 2^{\text{exponent - bias}}$$

2. A number in normalized scientific notation has a mantissa that has no leading 0's and must be of the form (1 + fraction) . For example, the binary representations 2.0×2^{-5}, 0.5×2^{-3}, 4.0×2^{-6}, and 1.0×2^{-4} are all equivalent but only 1.0×2^{-4} is the normalized scientific binary notation.
3. MIPS allows for two floating point representations: Single precision and double precision.
4. Single precision has a bias of 127 while double precision has a bias of 1023.
5. In single precision, the floating point representation is 32 bit long and has the following form

31	30	29	28	27	26	25	24	23	22	21	20	19	18	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
S	**exponent**								**fraction**																						
	(8 bits)								**(23 bits)**																						

where S represents the sign bit, which is 1 for negative numbers and 0 for positive numbers.

Activity 2:

Represent -0.75_{ten}, 1.4_{ten} in single precision of IEEE 754 binary representation.

Floating Point: Double Precision

1. In double precision, the value of bias in

$$(-1)^{S} \times (1 + \text{fraction})_{two} \times 2^{\text{exponent - bias}}$$

is 1023.

2. In single precision, the floating point representation is 64 bit long and has the following form

31	30	29	28	27	26	25	24	23	22	21	20	19	18	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
S	**exponent**											**fraction**																			
	(11 bits)											**(Total of 52 bits)**																			

31	30	29	28	27	26	25	24	23	22	21	20	19	18	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
fraction (continued)																															

Activity 3:

Represent -0.75_{ten} in double precision of IEEE 754 binary representation.

Activity 4:

Show that the largest magnitude that can be represented using single precision is $\pm 6.8_{ten} \times 10^{38}$, while the smallest fraction that can be represented is $\pm 5.9_{ten} \times 10^{-39}$.

Floating Point Registers

Name	Example	Comments
32 floating point registers each is 32 bits long	`$f0,$f1,$f2,$f3,$f4 ,…,$f31`	**MIPS floating point registers are used in pairs for double precision numbers**
Memory w/ 2^{30} words	**Memory[0], Memory[4], … Memory[4294967292]**	**Memory is accessed one floating point (single or double precision) at a time**

The following is the established register usage convention for the floating point registers:

`$f0,$f1,$f2,$f3:`	Function-returned values
`$f4,$f5,…, $f11:`	Temporary values
`$f12,$f13,$f14,$f15:`	Arguments passed into a function
`$f16,$f17,$f18,$f19:`	More Temporary values
`$f20,$f21,…, $f31:`	Saved values

Floating Point Instructions

Category	Instruction	Example	Meaning	Comments
Arithmetic	FP add single	add.s $f2,$f4,$f6	$f2 ← $f4+$f6	Single Prec.
	FP subtract single	sub.s $f2,$f4,$f6	$f2 ← $f4-$f6	Single Prec.
	FP multiply single	mul.s $f2,$f4,$f6	$f2 ← $f4×$f6	Single Prec.
	FP divide single	div.s $f2,$f4,$f6	$f2 ← $f4/$f6	Single Prec.
	FP add double	add.d $f2,$f4,$f6	$f2 ← $f4+$f6	Double Prec.
	FP subtract double	sub.d $f2,$f4,$f6	$f2 ← $f4-$f6	Double Prec.
	FP multiply double	mul.d $f2,$f4,$f6	$f2 ← $f4×$f6	Double Prec.
	FP divide double	div.d $f2,$f4,$f6	$f2 ← $f4/$f6	Double Prec.
Data Transfer	load word copr.1	lwc1 $f2,100($s2)	$f2 ← Mem[$s2+100]	Single Prec.
	store word copr.1	swc1 $f2,100($s2)	Mem[$s2+100] ← $f2	Single Prec.
Conditional branch	FP compare single (eq, ne, lt, le, gt, ge)	c.lt.s $f2,$f4	if($f2<$f4)cond = 1, else cond = 0	Single Prec.
	FP compare double (eq, ne, lt, le, gt, ge)	c.lt.d $f2,$f4	if($f2<$f4)cond = 1, else cond = 0	Double Prec.
	Branch on FP true	bc1t 25	if cond==1 go to PC+100+4	Single/ Double Prec.
	Branch on FP false	bc1f 25	if cond==0 go to PC+100+4	Single/ Double Prec.

Example

```
# calculate area of a circle
        .data
Ans:    .asciiz     "The area of the circle is: "
Ans_add:.word       Ans                         # Pointer to String (Ans)
Pi:     .double     3.1415926535897924
Rad:    .double     12.345678901234567
Rad_add:.word       Rad                         # Pointer to float (Rad)
      .text
main: lw $a0, Ans_add($0)           # load address of Ans into $a0
      addi $v0, $0, 4               # Sys Call 4 (Print String)
      syscall
#---------------                     # load float (Assembler Instruction)
      la $s0, Pi                    # load address of Pi into $s0
      ldc1 $f2, 0($s0)              # $f2 = Pi
#---------------                     # load float (MIPS Instruction)
      lw $s0, Rad_add($0)           # load address of Rad into $s0
      ldc1 $f4, 0($s0)              # $f4 = Rad
      mul.d $f12, $f4, $f4
      mul.d $f12, $f12, $f2
      addi $v0, $0, 3               # Sys Call 3 (Print Double)
      syscall
exit: jr $ra
```