

1. (5 points) An isotropic antenna radiates 3.33 W and its signal is picked up by an antenna 2.1 km away with an aperture area of 350 cm² and an efficiency of 0.8. We wish to receive the same amount of power with a second antenna that has an aperture of 120 cm² and an efficiency of 0.95. What is the maximum distance we can place the second antenna from the isotropic radiator? Assume the communication is at 900 MHz.

$$P_{r \text{ large}} = P_{r \text{ small}}$$

$$\frac{P_t G_t \eta_1 A_{e1}}{4\pi d_1^2} = \frac{P_t G_t \eta_2 A_{e2}}{4\pi d_2^2}$$

$$\frac{0.8 \times 350 \times 10^{-4}}{(2.1 \times 10^3)^2} = \frac{0.95 \times 120 \times 10^{-4}}{d_2^2}$$

$$d_2 = 1.34 \text{ km}$$

2. (5 points) A transmitter operates with an effective isotropic radiated power of 3 W and has a transmit gain of 1.2-dBd. It communicates with a receiver antenna 0.7 km away that has a gain of 4.1-dBi. If the communication occurs at 2.4 GHz what is the power at the output of the receive antenna in dBm?

$$P_r = \frac{P_t G_t G_r}{(4\pi d/\lambda)^2}$$

$$P_r / \text{dBm} = P_t / \text{dBm} + G_t / \text{dB} + G_r / \text{dB} - 20 \cdot \log \left(\frac{4\pi d}{\lambda} \right)$$

$$= 34.77 + 3.35 + 4.1 - 20 \cdot \log \left(\frac{4\pi \cdot 700}{0.125} \right)$$

$$= -54.7 \text{ dBm}$$

3. (5 points) A receiver has a noise figure of 7-dB and a power gain of 47-dB. It has a 400-kHz bandwidth and is attached to a 100-K antenna. What is the noise power coming out of the receiver (in Watts)? What is the total noise power contributed by the receiver electronics at the output (in Watts)?

$$\begin{aligned}
 P_{out} &= k(T_{ant} + T_e) \cdot G_o \cdot B & T_e &= T_{ant}(F - 1) \\
 &= k(501) \cdot 10^{4.7} \cdot 400 \times 10^3 & &= 100(10^{0.7} - 1) \\
 &= 1.39 \times 10^{-10} \text{ W} & &= 401 \text{ K}
 \end{aligned}$$

$$\begin{aligned}
 P_{out} /_{electronics} &= k T_e G_o \cdot B \\
 &= 1.11 \times 10^{-10} \text{ W}
 \end{aligned}$$

$$\begin{aligned}
 h &= 6.625 \times 10^{-34} \text{ J}\cdot\text{s}, \quad q = 1.6 \times 10^{-19} \text{ C}, \quad k = 1.38 \times 10^{-23} \text{ J/K}, \quad c = 3 \times 10^8 \text{ m/s} \\
 1 \text{ nW} &= 10^{-9} \text{ W}, \quad 1 \mu\text{W} = 10^{-6} \text{ W}
 \end{aligned}$$

$$E = hf, \quad f = c/\lambda, \quad d = v \cdot t$$

$$Q \text{ [dB]} = 10 \log(Q), \quad \log(A \cdot B/C) = \log(A) + \log(B) - \log(C)$$

$$P = V \cdot I, \quad V = R \cdot I$$

$$p = \frac{P_t}{4\pi d^2}, \quad P_r = p \cdot A_{er} = \frac{(EIRP)A_{er}}{4\pi d^2}$$

$$\text{beamwidth} = \frac{k\lambda}{L}$$

$$G = 4\pi\eta \frac{A_e}{\lambda^2}, \quad P_r = \frac{P_t G_t G_r \lambda^2}{(4\pi)^2 d^2}$$

$$P = kTB, \quad S(f) = \frac{N_0}{2}, \quad S_y(f) = |H(f)|^2 S_x(f), \quad P_y = \int_{-\infty}^{\infty} S_y(f) df$$

$$\langle v^2 \rangle = \lim_{T \rightarrow \infty} \frac{1}{T} \int_{T/2}^{T/2} v^2(t) dt, \quad v_{rms} = \sqrt{\langle v^2 \rangle}, \quad kTB = \langle v^2 \rangle / 4R, \quad \langle v^2 \rangle = 4kTRB = 4N_0RB$$

$$P_{ao} = G_o \cdot N_0 \cdot B = \frac{N_0}{2} \int_{-\infty}^{\infty} G(f) df, \quad G(f) = \frac{1}{1 + (f/f_{3dB})^{2n}}, \quad B = \frac{\pi/2 f_{3dB}}{n \sin(\frac{\pi}{2n})}$$

$$P_{ao} = G_o N_0 B F = kTB G_o F = k(T_0 + T_e) B G_o, \quad F = 1 + \frac{T_e}{T_0}, \quad T_e = T_0(F - 1)$$

$$F = F_1 + \frac{F_2 - 1}{G_{01}} + \frac{F_3 - 1}{G_{01} G_{02}}, \quad T_e = T_{e1} + \frac{T_{e2}}{G_{01}} + \frac{T_{e3}}{G_{01} G_{02}}$$

$$P_r \approx \frac{P_t G_t G_r \lambda^2}{(4\pi)^2 L_{sys}} \left(\frac{4\pi h_t h_r}{\lambda} \right)^2 \frac{1}{d^4}$$