

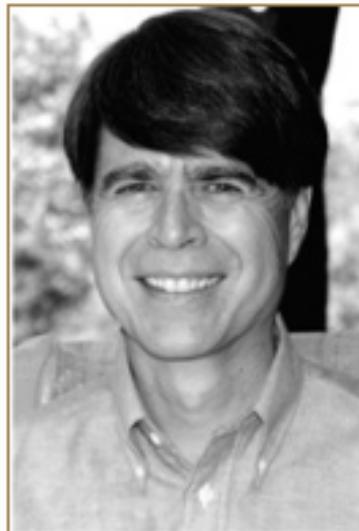
Earley's Algorithm (1970)



Nice combo of our parsing ideas so far:

- no restrictions on the form of the grammar:
 - A → B C spoon D x
- incremental parsing (left to right, like humans)
- left context constrains parsing of subsequent words
 - so waste less time building impossible things
 - makes it faster than $O(n^3)$ for many grammars

About Jay



Jay Earley, Ph.D., is a transformational psychologist, group leader, psychotherapist, coach, author, teacher, and theorist.

Jay is trained in Internal Family Systems Therapy and assists with professional trainings in IFS. He leads IFS Classes for the general public which teach IFS as a practice for self-help and peer counseling. He is active in the IFS community and has presented a number of workshops at IFS annual conferences. He also teaches classes on Communication from the Heart, based on IFS, interactive groups, and the Pattern System.

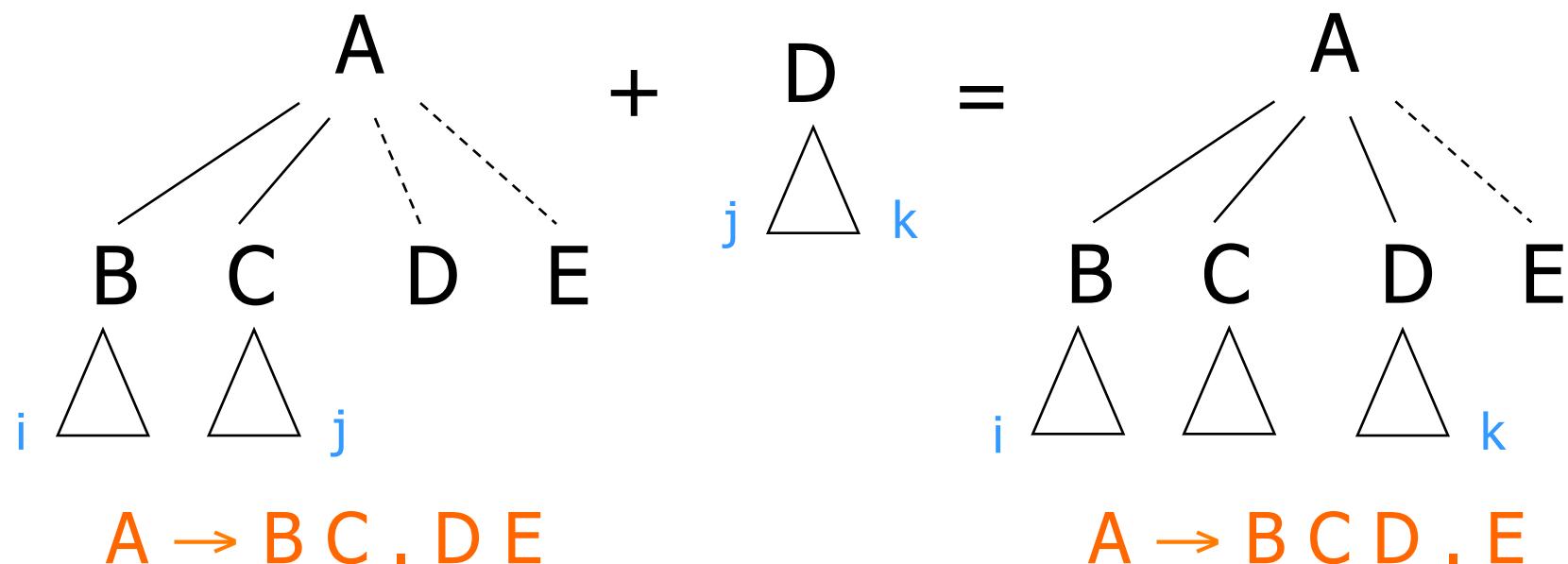
He is nationally known for his innovation in the group psychotherapy field. His book, *Interactive Group Therapy: Integrating Interpersonal, Action-Oriented, and Psychodynamic Approaches*, Brunner/Mazel, describes his group therapy method in which people learn interpersonal relationship skills by working directly on their relationships with each other. During his ten years on the east coast, Jay was Director of the Group Therapy Center of Long Island, where he trained group therapists in this method. He has written a number of articles on interactive groups and made numerous presentations at regional and national psychotherapy conferences. He continues to lead interactive therapy groups in the Bay Area.

Jay offers Life Purpose Coaching and Change Agent Coaching, on finding your life purpose and making a difference in the world. He has been writing about and leading workshops on Life Purpose since 1984. He has collected his writings on life purpose into an ebook *Finding Your Life Purpose*.

Jay also has a Ph.D. in computer science from Carnegie-Mellon University and was formerly on the U.C. Berkeley faculty, where he published 12 computer science papers, one of which was voted one of the best 25 papers of the quarter century by the Communications of the A.C.M.

Overview of Earley's Algorithm

- Finds constituents and partial constituents in input
 - $A \rightarrow B C . D E$ is partial: only the first half of the A



Overview of Earley's Algorithm



- Proceeds incrementally, left-to-right
 - Before it reads word 5, it has already built all hypotheses that are consistent with first 4 words
 - Reads word 5 & attaches it to immediately preceding hypotheses. Might yield new constituents that are then attached to hypotheses immediately preceding *them* ...
- E.g., attaching D to $A \rightarrow B C . D E$ gives $A \rightarrow B C D . E$
- Attaching E to that gives $A \rightarrow B C D E .$
- Now we have a complete A that we can attach to hypotheses immediately preceding the A, etc.

Our Usual Example Grammar

ROOT → S

S → NP VP NP → Papa

NP → Det N N → caviar

NP → NP PP N → spoon

VP → VP PP V → ate

VP → V NP P → with

PP → P NP Det → the

Det → a

0 Papa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

First Try: Recursive Descent

ROOT → S	VP → VP PP	NP → Papa	V → ate
S → NP VP	VP → V NP	N → caviar	P → with
NP → Det N	PP → P NP	N → spoon	Det → the
NP → NP PP			Det → a

- 0 ROOT → . S 0
 - 0 S → . NP VP 0
 - 0 NP → . Papa 0
 - 0 NP → Papa . 1
 - 0 S → NP . VP 1
 - 1 VP → . VP PP 1
 - 1 VP → . VP PP 1
 - 1 VP → . VP PP 1
 - 1 VP → . VP PP 1
 - oops, stack overflowed
- OK, let's pretend that didn't happen.
- Let's suppose we didn't see VP → VP PP, and used VP → V NP

0 Papa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

First Try: Recursive Descent

$\text{ROOT} \rightarrow S$	$\text{VP} \rightarrow V \text{ NP}$	$\text{NP} \rightarrow \text{Papa}$	$V \rightarrow \text{ate}$
$S \rightarrow \text{NP VP}$	$\text{VP} \rightarrow \text{VP PP}$	$N \rightarrow \text{caviar}$	$P \rightarrow \text{with}$
$\text{NP} \rightarrow \text{Det N}$	$\text{PP} \rightarrow P \text{ NP}$	$N \rightarrow \text{spoon}$	$\text{Det} \rightarrow \text{the}$
$\text{NP} \rightarrow \text{NP PP}$			$\text{Det} \rightarrow a$

- 0 ROOT → . S 0
 - 0 S → . NP VP 0
 - 0 NP → . Papa 0
 - 0 NP → Papa . 1
 - 0 S → NP . VP 1 after dot = nonterminal, so recursively look for it (“predict”)
 - 1 VP → . V NP 1 after dot = nonterminal, so recursively look for it (“predict”)
 - 1 V → . ate 1 after dot = terminal, so look for it in the input (“scan”)
 - 1 V → ate . 2 after dot = nothing, so parent’s subgoal is completed (“attach”)
 - 1 VP → V . NP 2 predict (next subgoal)
 - 2 NP → . . . 2
 - 2 NP → . . . 7
 - 1 VP → V NP . 7 do some more parsing and eventually ...
 - we complete the parent’s NP subgoal, so attach
 - attach again

0 Papa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

First Try: Recursive Descent

ROOT → S	VP → V NP	NP → Papa	V → ate
S → NP VP	VP → VP PP	N → caviar	P → with
NP → Det N	PP → P NP	N → spoon	Det → the
NP → NP PP			Det → a

- 0 ROOT → . S 0
 - 0 S → . NP VP 0
 - 0 NP → . Papa 0
 - 0 NP → Papa . 1
 - 0 S → NP . VP 1
 - 1 VP → . V NP 1 must backtrack to try predicting a different VP rule here instead
 - 1 V → . ate 1
 - 1 V → ate . 2
 - 1 VP → V . NP 2
 - 2 NP → 2
 - 2 NP → 7
 - 1 VP → V NP . 7

But how about the other parse?

0 Papa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

First Try: Recursive Descent

ROOT → S	VP → V NP	NP → Papa	V → ate
S → NP VP	VP → VP PP	N → caviar	P → with
NP → Det N	PP → P NP	N → spoon	Det → the
NP → NP PP			Det → a

- 0 ROOT → . S 0
 - 0 S → . NP VP 0
 - 0 NP → . Papa 0
 - 0 NP → Papa . 1
 - 0 S → NP . VP 1
 - 1 VP → . VP PP 1
 - 1 VP → . V NP 1
 - 1 V → . ate 1
 - 1 V → ate . 2
 - 1 VP → V . NP 2
 - 2 NP → 2 do some more parsing and eventually ...
 - 2 NP → 4 ... the correct NP is from 2 to 4 this time
(but might we find the one from 2 to 7 instead?)

0 Papa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

First Try: Recursive Descent

ROOT → S	VP → V NP	NP → Papa	V → ate
S → NP VP	VP → VP PP	N → caviar	P → with
NP → Det N	PP → P NP	N → spoon	Det → the
NP → NP PP			Det → a

- 0 ROOT → . S 0
 - 0 S → . NP VP 0
 - 0 NP → . Papa 0
 - 0 NP → Papa . 1
 - 0 S → NP . VP 1
 - 1 VP → . VP PP 1
 - 1 VP → . VP PP 1
 - 1 VP → . VP PP 1
 - 1 VP → . VP PP 1
 - 1 VP → . VP PP 1

oops, stack overflowed

no fix after all

600.465 - Intro to NLP - J. Eisner – must transform grammar to eliminate left-recursive rules 10

Use a Parse Table (= “Chart”)



- Earley’s algorithm resembles recursive descent, but solves the left-recursion problem. No recursive function calls.
- Use a parse table as we did in CKY, so we can look up anything we’ve discovered so far.
“Dynamic programming.”
- Entries in column 5 look like $(3, S \rightarrow NP . VP)$
(but we’ll omit the \rightarrow etc. to save space)
 - Built while processing word 5
 - Means that the input substring from 3 to 5 matches the initial NP portion of a $S \rightarrow NP VP$ rule
 - Dot shows how much we’ve matched as of column 5
 - Perfectly fine to have entries like $(3, S \rightarrow is\ it\ .\ true\ that\ S)$

Use a Parse Table (“Chart”)

- Entries in column 5 look like $(3, S \rightarrow NP . VP)$
- **What does it mean if we have this entry?**
 - *Unknown right context*: Doesn't mean we'll necessarily be able to find a VP starting at column 5 to complete the S.
 - *Known left context*: Does mean that some dotted rule back in column 3 is looking for an S that starts at 3.
 - So if we actually do find a VP starting at column 5, allowing us to complete the S, then we'll be able to attach the S to something.
 - And when that something is complete, it too will have a customer to *its* left ... just as in recursive descent!
 - In short, a top-down (i.e., goal-directed) parser: it chooses to start building a constituent not because of the input but because that's what the left context needs. In **the spoon**, won't build **spoon** as a verb because there's no way to use a verb there.
 - So any hypothesis in column 5 *could* get used in the correct parse, if words 1-5 are continued in just the right way by words 6-n.

Operation of the Algorithm



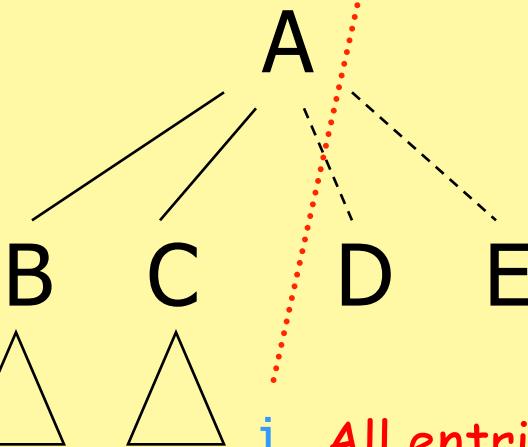
- Process all hypotheses one at a time in order.
(**Current hypothesis** is shown in blue, with **substring**.)
- This may add **new hypotheses** to the end of the to-do list, or try to add **old hypotheses** again.
- Process a hypothesis according to what follows the dot – just as in recursive descent:
 - If a word, **scan** input and see if it matches
 - If a nonterminal, **predict** ways to match it
(we'll predict blindly, but could reduce # of predictions by *looking ahead* k symbols in the input and only making predictions that are compatible with this limited *right context*)
 - If nothing, then we have a complete constituent, so **attach** it to all its **customers** (shown in purple).

One entry (hypothesis) ...

column j

$(i, A \rightarrow B C . D E)$
current hypothesis (incomplete)

which action?



All entries ending at j stored in column j, as in CKY

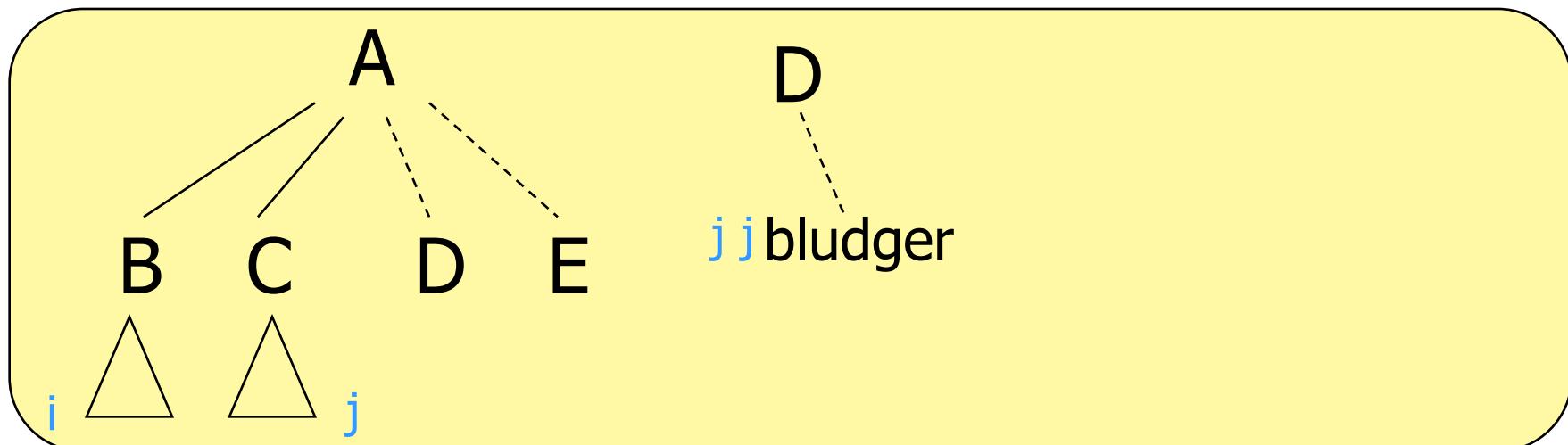
Predict

column j

(i, A → B C. D E)
current hypothesis (incomplete)

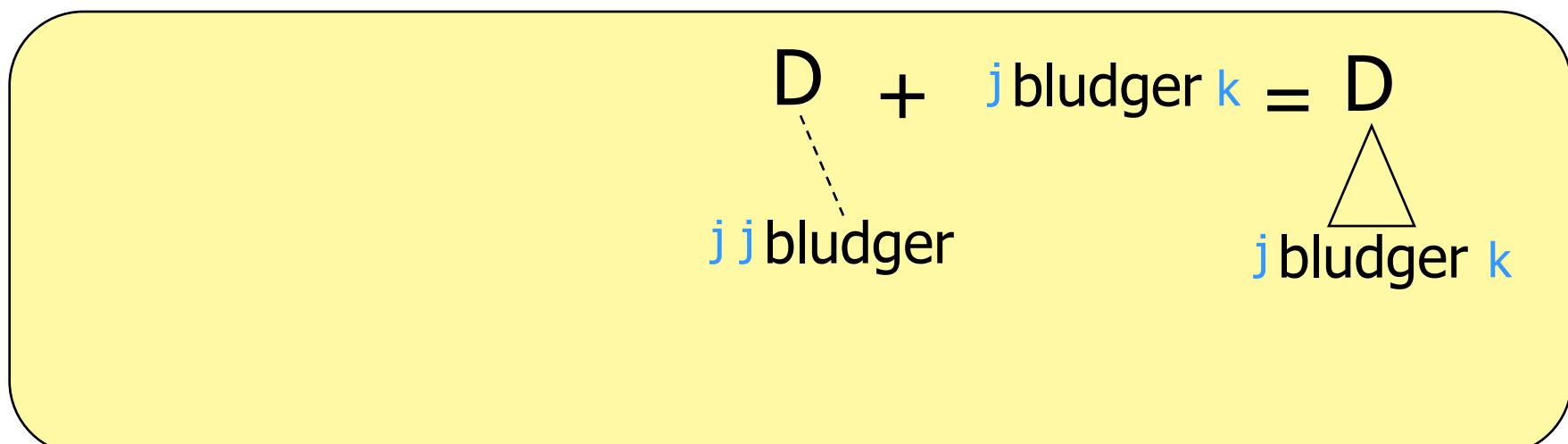
(j, D → . bludger)

new entry to process later



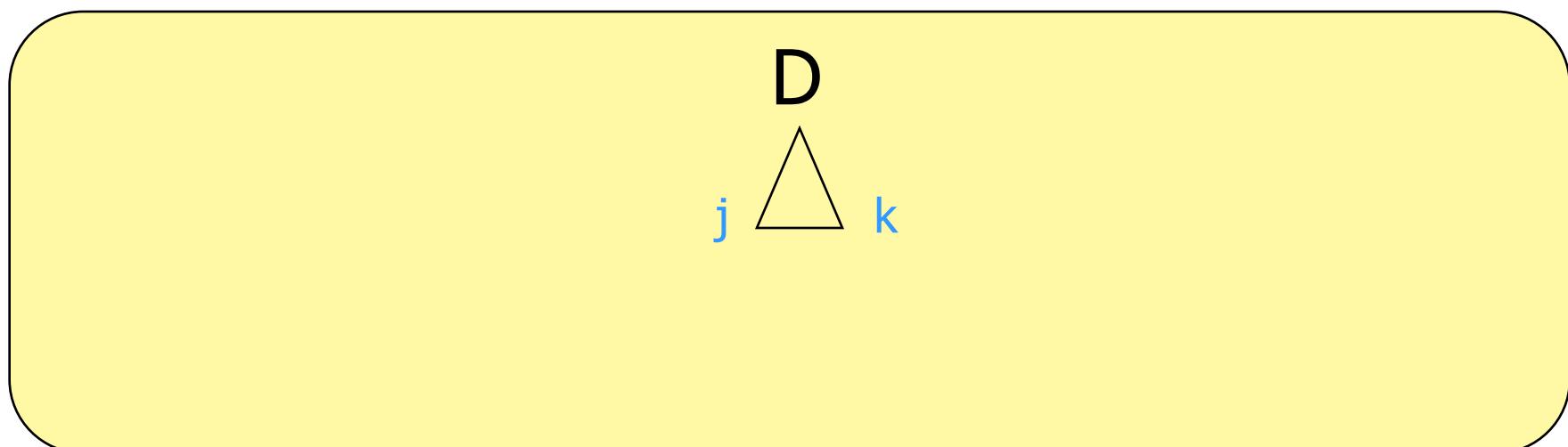
Scan

column j	...	column k	
$(i, A \rightarrow B C . D E)$ $(j, D \rightarrow . bludger)$ Current hypothesis (incomplete)	...	$(j, D \rightarrow bludger .)$ new entry to process later	<p style="text-align: right;">k=j+1 in this example</p>



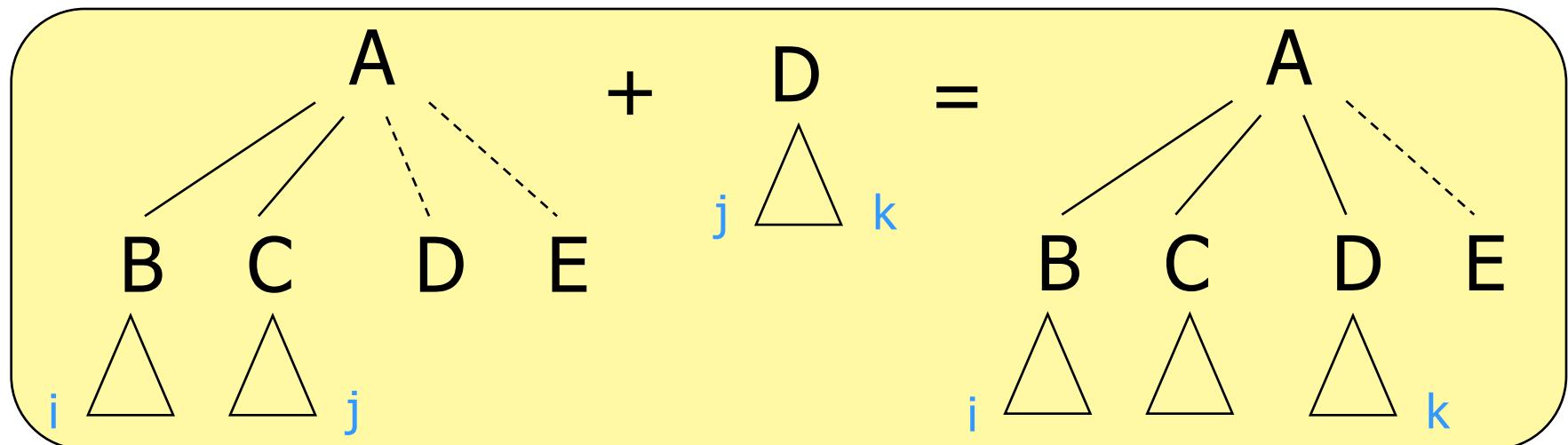
Attach

column j	...	column k
(i, A → B C . D E)		(j, D → bludger .) current hypothesis (complete)



Attach

column j	...	column k
$(i, A \rightarrow B C . D E)$ customer (incomplete)		$(j, D \rightarrow \text{bludger}.)$ current hypothesis (complete) $(i, A \rightarrow B C D . E)$ new entry to process later



₀ Papa ₁ ate ₂ the ₃ caviar ₄ with ₅ a ₆ spoon ₇

Our Usual Example Grammar

ROOT → S

S → NP VP NP → Papa

NP → Det N N → caviar

NP → NP PP N → spoon

VP → VP PP V → ate

VP → V NP P → with

PP → P NP Det → the

Det → a

0
0 ROOT . S

initialize

Remember this stands for (0, ROOT → . S)

0
0 ROOT . S
0 S . NP VP

predict the kind of S we are looking for

Remember this stands for (0, S → . NP VP)

0
0 ROOT . S
0 S . NP VP
0 NP . Det N
0 NP . NP PP
0 NP . Papa

predict the kind of NP we are looking for
(actually we'll look for 3 kinds: any of the 3 will do)

0
0 ROOT . S
0 S . NP VP
0 NP . Det N
0 NP . NP PP
0 NP . Papa
0 Det . the
0 Det . a

predict the kind of Det we are looking for (*2 kinds*)

0
0 ROOT . S
0 S . NP VP
0 NP . Det N
0 NP . NP PP
0 NP . Papa
0 Det . the
0 Det . a

predict the kind of NP we're looking for
*but we were already looking for these so
don't add duplicate goals! Note that this happened
when we were processing a left-recursive rule.*

scan: the desired word is in the input!

scan: failure

scan: failure

0	Papa	1
0 ROOT . S	0 NP Papa .	
0 S . NP VP	0 S NP . VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP		
0 NP . Papa		
0 Det . the		
0 Det . a		

attach the newly created NP
 (which starts at 0) to its **customers**
 (incomplete constituents that *end* at 0
 and have NP after the dot)

predict

0	Papa	1
0 ROOT . S	0 NP Papa .	
0 S . NP VP	0 S NP . VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP	1 VP . V NP	
0 NP . Papa	1 VP . VP PP	
0 Det . the	1 PP . P NP	
0 Det . a		

predict

0	Papa	1
0 ROOT . S	0 NP Papa .	
0 S . NP VP	0 S NP . VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP	1 VP . V NP	
0 NP . Papa	1 VP . VP PP	
0 Det . the	1 PP . P NP	
0 Det . a	1 V . ate	

predict

predict

predict

scan: success!

scan: failure

attach

predict

predict (*these next few steps
should look familiar*)

predict

scan (*this time we fail since
Papa is not the next word*)

scan: success!

0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .		2 Det the .		3 N caviar .		
0 S . NP VP	0 S NP . VP	1 VP V . NP		2 NP Det . N		2 NP Det N .		
0 NP . Det N	0 NP NP . PP	2 NP . Det N		3 N . caviar				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		3 N . spoon				
0 NP . Papa	1 VP . VP PP	2 NP . Papa						
0 Det . the	1 PP . P NP	2 Det . the						
0 Det . a	1 V . ate	2 Det . a						
	1 P . with							

attach

0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .		2 Det the .		3 N caviar .		
0 S . NP VP	0 S NP . VP	1 VP V . NP		2 NP Det . N		2 NP Det N .		
0 NP . Det N	0 NP NP . PP	2 NP . Det N		3 N . caviar		1 VP V NP .		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		3 N . spoon		2 NP NP . PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa						
0 Det . the	1 PP . P NP	2 Det . the						
0 Det . a	1 V . ate	2 Det . a						
	1 P . with							

attach
(again!)

0	Papa	1	ate	2	the	3	caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .		2 Det the .		3 N caviar .		
0 S . NP VP	0 S NP . VP	1 VP V . NP		2 NP Det . N		2 NP Det N .		
0 NP . Det N	0 NP NP . PP	2 NP . Det N		3 N . caviar		1 VP V NP .		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		3 N . spoon		2 NP NP . PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa				0 S NP VP .		
0 Det . the	1 PP . P NP	2 Det . the				1 VP VP . PP		
0 Det . a	1 V . ate	2 Det . a						
	1 P . with							

attach
(again!)

attach *(again!)*

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .		2 Det the .		3 N caviar 6 N spoon .	
0 S . NP VP	0 S NP . VP	1 VP V . NP		2 NP Det . N		2 NP Det N .			5 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N		3 N . caviar		1 VP V NP .			4 PP P NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		3 N . spoon		2 NP NP . PP			5 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa				0 S NP VP .			2 NP NP PP .	
0 Det . the	1 PP . P NP	2 Det . the				1 VP VP . PP			1 VP VP PP .	
0 Det . a	1 V . ate	2 Det . a				4 PP . P NP			7 PP . P NP	
	1 P . with					0 ROOT S .			1 VP V NP .	
						4 P . with			2 NP NP . PP	
									0 S NP VP .	
									1 VP VP . PP	
									7 P . with	
									0 ROOT S .	

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .		2 Det the .		3 N caviar 6 N spoon .	
0 S . NP VP	0 S NP . VP	1 VP V . NP		2 NP Det . N		3 N Det N .			5 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N		3 N . caviar		1 VP V NP .			4 PP P NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		3 N . spoon		2 NP NP . PP			5 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa				0 S NP VP .			2 NP NP PP .	
0 Det . the	1 PP . P NP	2 Det . the				1 VP VP . PP			1 VP VP PP .	
0 Det . a	1 V . ate	2 Det . a				4 PP . P NP			7 PP . P NP	
	1 P . with					0 ROOT S .			1 VP V NP .	
						4 P . with			2 NP NP . PP	
									0 S NP VP .	
									1 VP VP . PP	
									7 P . with	
									0 ROOT S .	

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .		2 Det the .	3 N caviar 6 N spoon .	
0 S . NP VP	0 S NP . VP	1 VP V . NP		2 NP Det . N	2 NP Det N .				5 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N		3 N . caviar	1 VP V NP .				4 PP P NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		3 N . spoon	2 NP NP . PP				5 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa			0 S NP VP .				2 NP NP PP .	
0 Det . the	1 PP . P NP	2 Det . the				1 VP VP . PP			1 VP VP PP .	
0 Det . a	1 V . ate	2 Det . a				4 PP . P NP			7 PP . P NP	
	1 P . with					0 ROOT S .			1 VP V NP .	
						4 P . with			2 NP NP . PP	
									0 S NP VP .	
									1 VP VP . PP	
									7 P . with	
									0 ROOT S .	

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .		2 Det the .		3 N caviar 6 N spoon .	
0 S . NP VP	0 S NP . VP	1 VP V . NP		2 NP Det . N		2 NP Det N .			5 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N		3 N . caviar		1 VP V NP .			4 PP P NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		3 N . spoon		2 NP NP . PP			5 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa				0 S NP VP .			2 NP NP PP .	
0 Det . the	1 PP . P NP	2 Det . the				1 VP VP . PP			1 VP VP PP .	
0 Det . a	1 V . ate	2 Det . a				4 PP . P NP			7 PP . P NP	
	1 P . with					0 ROOT S .			1 VP V NP .	
						4 P . with			2 NP NP . PP	
									0 S NP VP .	
									1 VP VP . PP	
									7 P . with	
									0 ROOT S .	

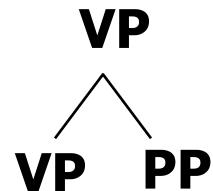
0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .		2 Det the .	3 N caviar 6 N spoon .	
0 S . NP VP	0 S NP . VP	1 VP V . NP		2 NP Det . N	2 NP Det N .				5 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N		3 N . caviar	1 VP V NP .				4 PP P NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		3 N . spoon	2 NP NP . PP				5 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa			0 S NP VP .				2 NP NP PP .	
0 Det . the	1 PP . P NP	2 Det . the				1 VP VP . PP			1 VP VP PP .	
0 Det . a	1 V . ate	2 Det . a				4 PP . P NP			7 PP . P NP	
	1 P . with					0 ROOT S .			1 VP V NP .	
						4 P . with			2 NP NP . PP	
									0 S NP VP .	
									1 VP VP . PP	
									7 P . with	
									0 ROOT S .	

Left Recursion Kills Pure Top-Down Parsing ...

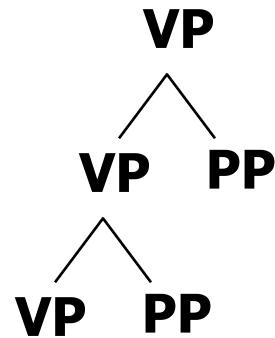


VP

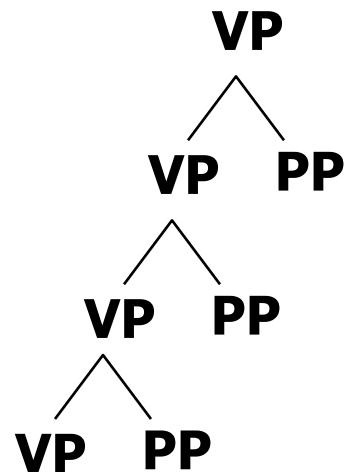
Left Recursion Kills Pure Top-Down Parsing ...



Left Recursion Kills Pure Top-Down Parsing ...



Left Recursion Kills Pure Top-Down Parsing ...



makes new hypotheses
ad infinitum before we've
seen the PPs at all

hypotheses try to predict
in advance how many
PP's will arrive in input

... but Earley's Alg is Okay!

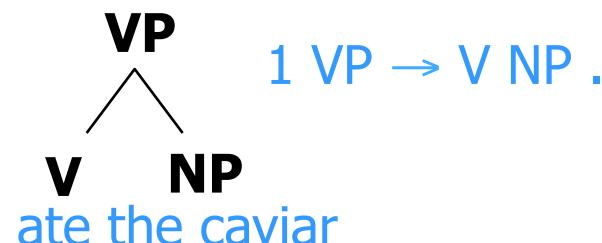


(in column 1)

... but Earley's Alg is Okay!

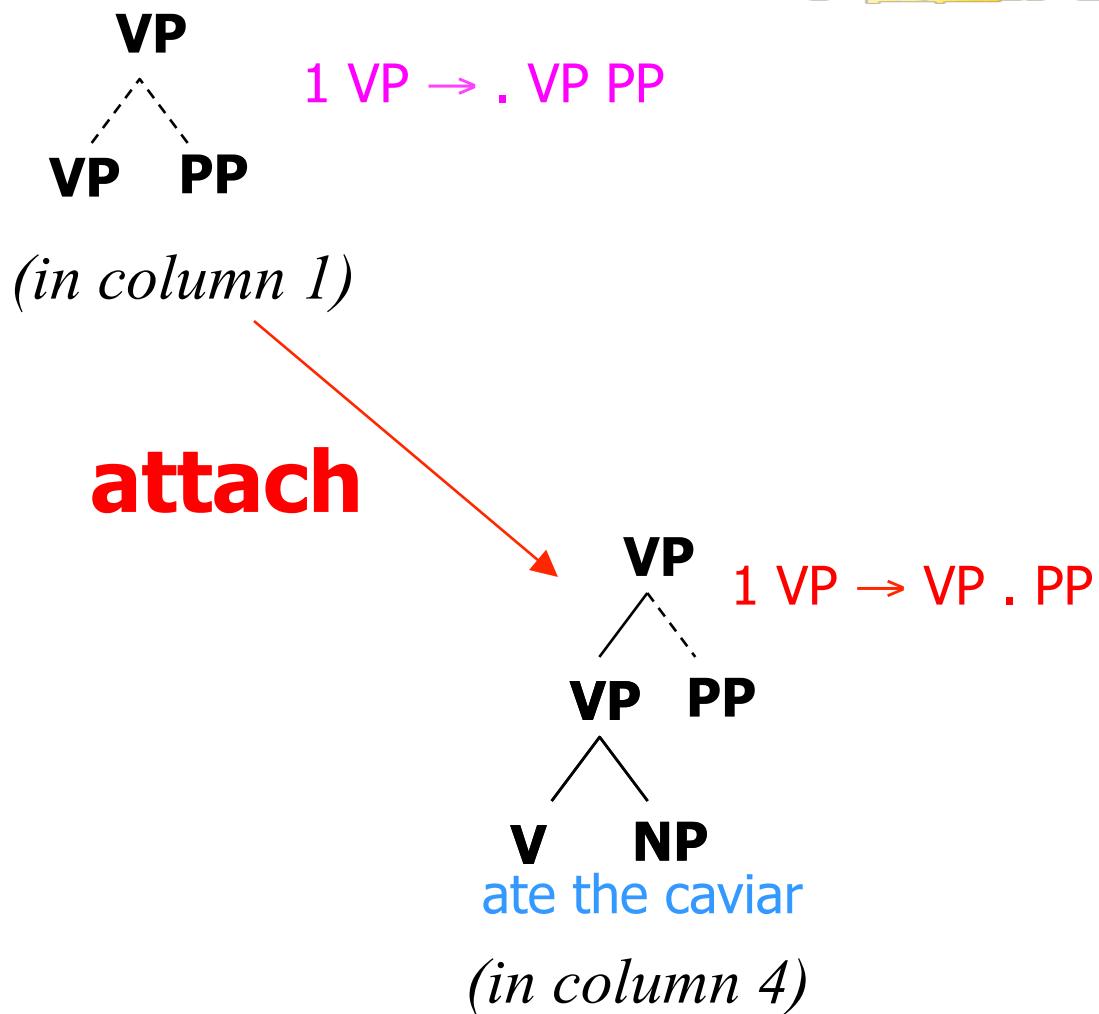


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(in column 4)

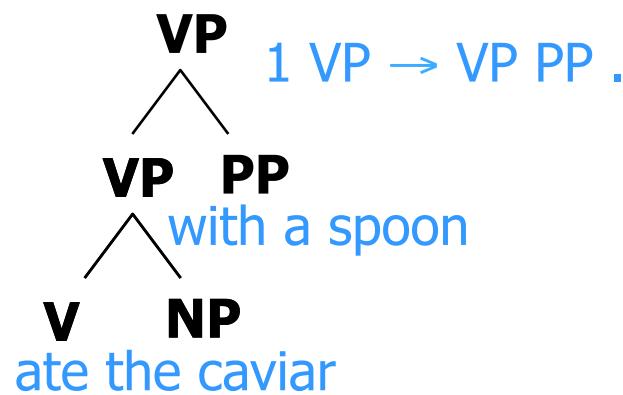
... but Earley's Alg is Okay!



... but Earley's Alg is Okay!



(in column 1)

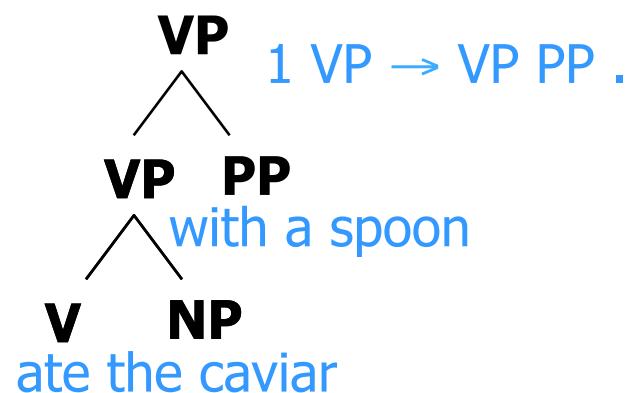


(in column 7)

... but Earley's Alg is Okay!



(in column 1)



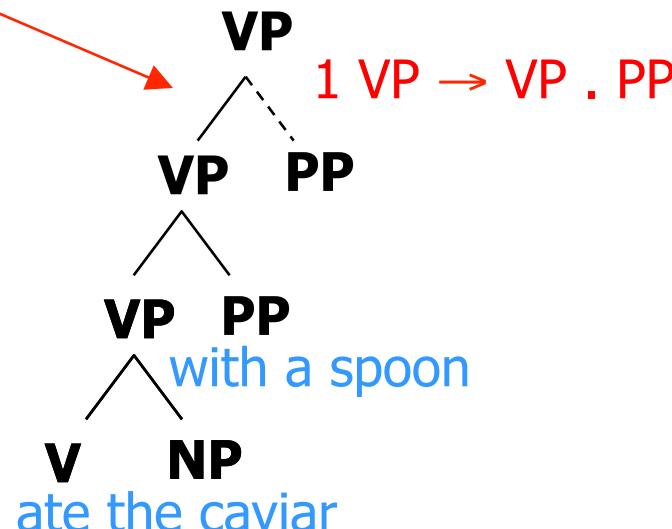
(in column 7)

... but Earley's Alg is Okay!



(in column 1)

attach

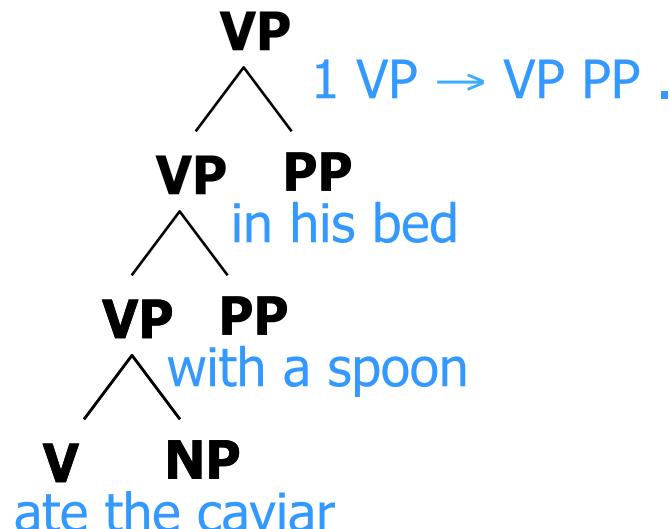


(in column 7)

... but Earley's Alg is Okay!



(in column 1)

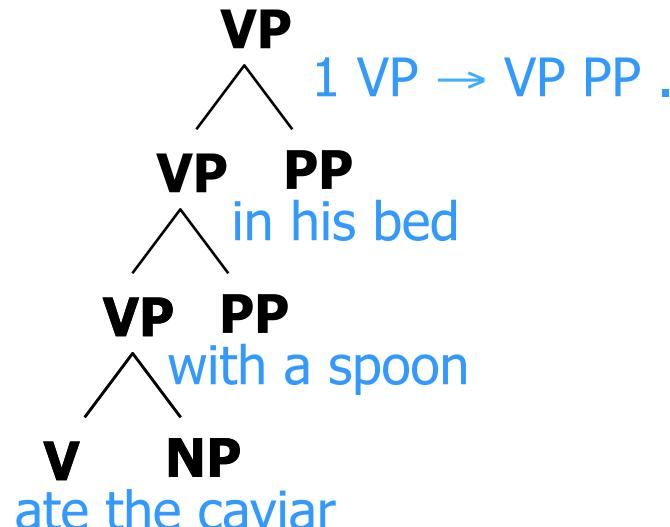


(in column 10)

... but Earley's Alg is Okay!

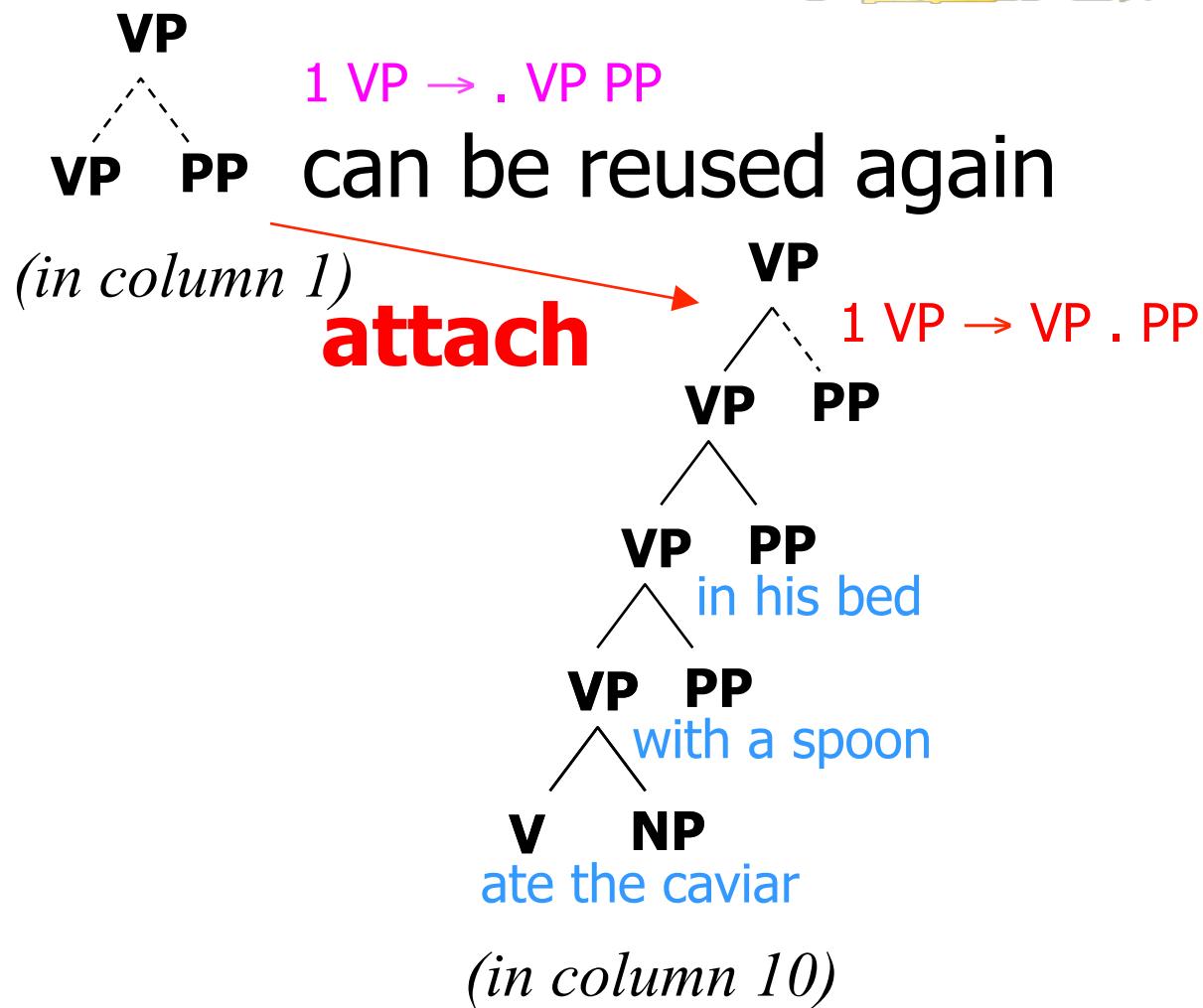


(in column 1)



(in column 10)

... but Earley's Alg is Okay!



0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .		2 Det the .		3 N caviar 6 N spoon .	
0 S . NP VP	0 S NP . VP	1 VP V . NP		2 NP Det . N		2 NP Det N .			5 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N		3 N . caviar		1 VP V NP .			4 PP P NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		3 N . spoon		2 NP NP . PP			5 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa				0 S NP VP .			2 NP NP PP .	
0 Det . the	1 PP . P NP	2 Det . the				1 VP VP . PP			1 VP VP PP .	
0 Det . a	1 V . ate	2 Det . a				4 PP . P NP			7 PP . P NP	
	1 P . with					0 ROOT S .			1 VP V NP .	
						4 P . with			2 NP NP . PP	
completed a VP in col 4										
col 1 lets us use it in a VP PP structure										
									0 S NP VP .	
									1 VP VP . PP	
									7 P . with	
									0 ROOT S .	

0	Papa	1	ate	2	the	3	caviar	4	with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .		2 Det the .		3 N caviar 6 N spoon .	
0 S . NP VP	0 S NP . VP	1 VP V . NP		2 NP Det . N		2 NP Det N .			5 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N		3 N . caviar		1 VP V NP .			4 PP P NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		3 N . spoon		2 NP NP . PP			5 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa				0 S NP VP .			2 NP NP PP .	
0 Det . the	1 PP . P NP	2 Det . the				1 VP VP . PP			1 VP VP PP .	
0 Det . a	1 V . ate	2 Det . a				4 PP . P NP			7 PP . P NP	
	1 P . with					0 ROOT S .			1 VP V NP .	
						4 P . with			2 NP NP . PP	
									0 S NP VP .	
									1 VP VP . PP	
									7 P . with	
									0 ROOT S .	

completed that VP = VP PP in col 7
 col 1 would let us use *it* in a VP PP structure
 can reuse col 1 as often as we need

What's the Complexity?

