Cache Performance

- CPUtime = Instruction count x CPI x Clock cycle time
- CPIexecution = CPI with ideal memory
- CPI = CPIexecution + Mem Stall cycles per instruction
- Mem Stall cycles per instruction =

Mem accesses per instruction x Miss rate x Miss penalty

- CPUtime = Instruction Count x (CPIexecution + Mem Stall cycles per instruction) x Clock cycle time
- CPUtime = IC x (CPIexecution + Mem accesses per instruction x Miss rate x Miss penalty) x Clock cycle time
- Misses per instruction = Memory accesses per instruction x Miss rate
- CPUtime = IC x (CPIexecution + Misses per instruction x Miss penalty) x Clock cycle time

Cache Performance

- Assuming the following execution and cache parameters:
  - Cache miss penalty = 50 cycles
  - Normal instruction execution CPI ignoring memory stalls = 2.0 cycles
  - Miss rate = 2%
  - Average memory references/instruction = 1.33
- CPU time = IC × [CPI execution + Memory accesses/instruction × Miss rate × Miss penalty] × Clock cycle time
- CPUtime with cache = IC x (2.0 + (1.33 x 2% x 50)) x clock cycle time
- = IC x 3.33 x Clock cycle time
- *Lower CPI execution increases the impact of cache miss clock cycles*

Cache Performance

- Suppose a CPU executes at Clock Rate = 200 MHz (5 ns per cycle) with a single level of cache.
- CPIexecution = 1.1
- Instruction mix: 50% arith/logic, 30% load/store, 20% control
- Assume a cache miss rate of 1.5% and a miss penalty of 50 cycles.
- CPI = $\text{CPI}_{\text{execution}}$ + mem stalls per instruction
- Mem Stalls per instruction =
- Mem accesses per instruction x Miss rate x Miss penalty
- Mem accesses per instruction = 1 + .3 = 1.3
- Mem Stalls per instruction = 1.3 x .015 x 50 = 0.975
- CPI = 1.1 + .975 = 2.075
- The ideal memory CPU with no misses is 2.075/1.1 = 1.88 times faster

Cache Performance

- Suppose for the previous example we double the clock rate to 400 MHZ, how much faster is this machine, assuming similar miss rate, instruction mix?
- Since memory speed is not changed, the miss penalty takes more CPU cycles:
- Miss penalty = 50 x 2 = 100 cycles.
- CPI = 1.1 + 1.3 x .015 x **100** = 1.1 + 1.95 = 3.05
- Speedup = (CPIold x Cold)/ (CPInew x Cnew)
- = 2.075 x 2 / 3.05 = 1.36
- The new machine is only 1.36 times faster rather than 2

times faster due to the increased effect of cache misses.

- *CPUs with higher clock rate, have more cycles per cache miss and more memory impact on CPI.*

Cache Performance

- Suppose a CPU uses separate level one (L1) caches for instructions and data (Harvard memory architecture) with different miss rates for instruction and data access:
  - $CPI_{execution}$ = 1.1
  - Instruction mix: 50% arith/logic, 30% load/store, 20% control
  - Assume a cache miss rate of 0.5% for instruction fetch and a cache data miss rate of 6%.
  - A cache hit incurs no stall cycles while a cache miss incurs 200 stall cycles for both memory reads and writes. Find the resulting CPI using this cache? How much faster is the CPU with ideal memory?

CPI = $CPI_{execution}$ + mem stalls per instruction

Mem Stall cycles per instruction = Instruction Fetch Miss rate x Miss Penalty + Data Memory Accesses Per Instruction x Data Miss Rate x Miss Penalty

Mem Stall cycles per instruction = 1 x 0.5/100 x 200 + 0.3 x 6/100 x 200 = 1 + 3.6 = 4.6

CPI = $CPI_{execution}$ + mem stalls per instruction = 1.1 + 4.6 = 5.7

The CPU with ideal cache (no misses) is 5.7/1.1 = 5.18 times faster

With no cache the CPI would have been = 1.1 + 1.3 X 200 = 261.1

Cache Performance

Size	Instruction cache	Data cache	Unified cache
1 KB	3.06%	24.61%	13.34%
2 KB	2.26%	20.57%	9.78%
4 KB	1.78%	15.94%	7.24%
8 KB	1.10%	10.19%	4.57%
16 KB	0.64%	6.47%	2.87%
32 KB	0.39%	4.82%	1.99%
64 KB	0.15%	3.77%	1.35%
128 KB	0.02%	2.88%	0.95%

Write Policy

1 Write Though: Data is written to both the cache block and to a block of main memory.

- The lower level always has the most updated data; an important feature for I/O and multiprocessing.
- Easier to implement than write back.
- A write buffer is often used to reduce CPU write stall while data is written to memory.

2 Write back: Data is written or updated only to the cache block. The modified or dirty cache block is written to main memory when it's being replaced from cache.

- Writes occur at the speed of cache
- A status bit called a dirty or modified bit, is used to indicate whether the block was modified while in cache; if not the block is not written back to main memory when replaced.
- Uses less memory bandwidth than write through.

Write Policy

Write Allocate:

The cache block is loaded on a write miss followed by write hit actions.

No-Write Allocate:

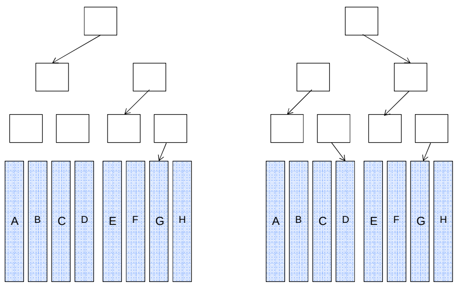
The block is modified in the lower level (lower cache level, or main

memory) and not loaded into cache.

LRU

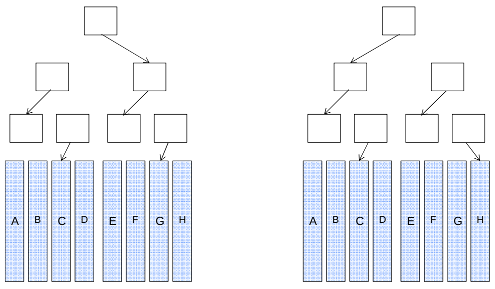
- A list to keep track of the order of access to every block in the set.
- The least recently used block is replaced (if needed).
- How many bits we need for that?

Pseudo LRU



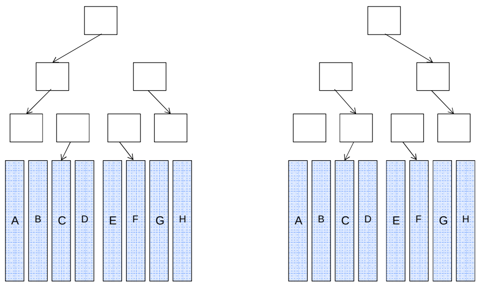
H HC

Psuedo LRU



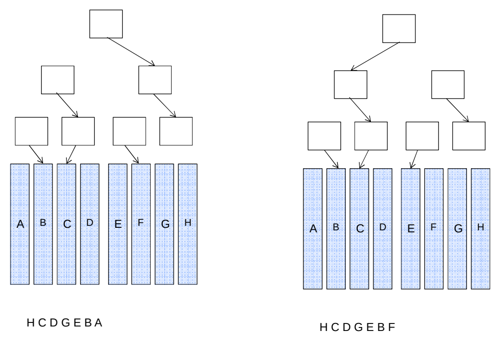
H C D H C D G

Psuedo LRU



H C D G E H C D G E B

Psuedo LRU



Example

- Which has a lower miss rate 16KB cache for both instruction or data, or a combined 32KB cache? (0.64%, 6.47%, 1.99%).
- Assume hit=1cycle and miss =50 cycles. 75% of memory references are $\underline{\text{instruction fetch}}$. reads
- Miss rate of split cache=$\underline{0.75*0.64\%}$+$\underline{0.25*6.47\%}$=2.1%
- Slightly worse than 1.99% for combined cache. But, what about average memory access time?
- Split cache: 75%(1+0.64%*50)+25%(1+6.47%*50) = 2.05 cycles.
- Combined cache: $\underline{75\%(1+1.99\%*50)}$+$\underline{25\%(1+\textbf{1}+1.99\%*50)}$ = 2.24

Extra cycle for load/store

Example

- A CPU with $CPI_{execution}$ = 1.1 Mem accesses per instruction = 1.3
- Uses a unified L1 Write Through, No Write Allocate, with:
  - No write buffer.
  - Perfect Write buffer
  - A realistic write buffer that eliminates 85% of write stalls
- Instruction mix: 50% arith/logic, 15% load, 15% store, 20% control
- Assume a cache miss rate of 1.5% and a miss penalty of 50 cycles.

$$CPI = CPI_{execution} + \text{mem stalls per instruction}$$

% reads = 1.15/1.3 = 88.5% % writes = .15/1.3 = 11.5%

Example

- A CPU with $CPI_{execution}$ = 1.1 uses a unified L1 with with write back, with write allocate, and the probability a cache block is dirty = 10%
- Instruction mix: 50% arith/logic, 15% load, 15% store, 20% control
- Assume a cache miss rate of 1.5% and a miss penalty of 50 cycles.

1.3 mem refs / inst

$$\frac{1.5}{100}\left(1.3 \times 50 \times 0.9 + 1.3 \times 0.1 \times \overset{50+50}{100}\right)$$

Example

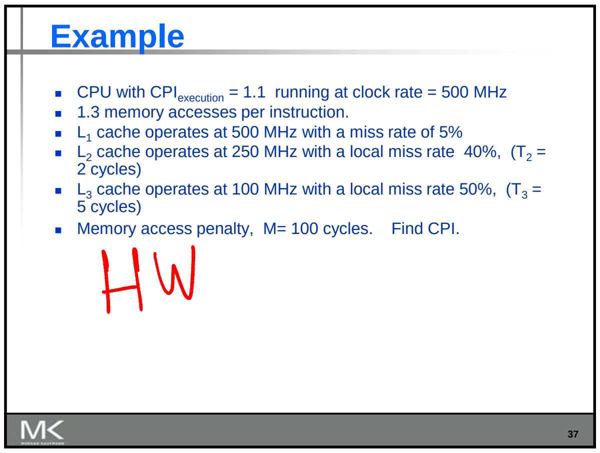
- CPU with $CPI_{execution}$ = 1.1 running at clock rate = 500 MHz
- 1.3 memory accesses per instruction.
- L_1 cache operates at 500 MHz with a miss rate of 5%
- L_2 cache operates at 250 MHz with local miss rate 40%, (T_2 = 2 cycles)
- Memory access penalty, M = 100 cycles. Find CPI.

$$1.3\left(\frac{5}{100} \times 0.6 \times 2 + \frac{5}{100} \times 0.4 \times 100\right)$$

Example

- CPU with $CPI_{execution}$ = 1.1 running at clock rate = 500 MHz
- 1.3 memory accesses per instruction.
- For L_1 :
  - Cache operates at 500 MHz with a miss rate of 1-H1 = 5%
  - Write though to L_2 with perfect write buffer with write allocate
- For L_2:
  - Cache operates at 250 MHz with local miss rate 1- H2 = 40%, (T_2 = 2 cycles)
  - Write back to main memory with write allocate
  - Probability a cache block is dirty = 10%
- Memory access penalty, M = 100 cycles. Find CPI.

$$0.05\left(0.6 \times 2 + 0.4 \times 0.9 \times 100 + 0.4 \times 0.1 \times 200\right)$$



Example

- CPU with $CPI_{execution} = 1.1$ running at clock rate = 500 MHz
- 1.3 memory accesses per instruction.
- L_1 cache operates at 500 MHz with a miss rate of 5%
- L_2 cache operates at 250 MHz with a local miss rate 40%, (T_2 = 2 cycles)
- L_3 cache operates at 100 MHz with a local miss rate 50%, (T_3 = 5 cycles)
- Memory access penalty, M= 100 cycles. Find CPI.

HW